

# DIRECT TORQUE CONTROL OF INDUCTION MOTOR USING FUZZY SLIDING MODE CONTROL

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## ABSTRACT

Direct torque control (DTC) is one of the control strategies of the Torque control of Induction machine. Sliding Mode Control (SMC) is known for its capability to cope with bounded disturbance as well as model imprecision which makes it ideal for the robust nonlinear control of IM drives. In this Paper Direct torque control (DTC) of the induction motor controlled by two fuzzy logic based sliding mode controllers. The aim is to control effectively the torque and flux. Torque control of an induction machine based on DTC strategy has been developed using Ziegler-Nichols (ZN), fuzzy sliding mode1 (FSM1) and fuzzy sliding mode2 (FSM2) speed controllers and a comprehensive study is presented in this paper. The model is constructed and simulated by using Matlab/Simulink for different operating conditions such as reference speed. Several numerical simulations have been carried out in a steady state and transient operation on a speed control mode. The results shows that the FSM2 gives better performance with less ITAE

**Keywords:** DTC, Fuzzy Logic, Induction Motor, Sliding Mode Control (SMC)

## I INTRODUCTION

The most common form of electromechanical drive for industrial, commercial and domestic applications is an Induction machine due to its cost, reliability and performance. Induction machines have simpler and more rugged structure, higher maintainability and economy than DC motors [1]. Basically, there are two types of instantaneous electromagnetic torque-controlled AC drives used for high performance applications. They are Vector Control (Field oriented control) and Direct Torque control. Based on operating principles these two methods are different, but their aims are same. Vector Control is based on stator current control in the field rotating reference using PWM inverter control. And Direct Torque Control (DTC) is based on stator flux control in the stator fixed reference frame using direct control of the inverter switching.

Due to its quick torque response, simplicity and robustness against rotor parameters variation, there has been a fast growth in industrial applications of the DTC technique. This is compared with a vector control scheme; DTC provides similar dynamic performance with simpler controller architecture [2]. The basic block diagram of the direct torque control of three-phase induction motors with a speed control loop is shown in Fig.1. because of simple structure and satisfactory performance over a wide range of operation, PID Controller is the most common choice for the speed controller shown in Fig. 1. The main problem of that simple controller is the correct choice of the PID gains and the fact that by using fixed gains, the controller may not provide the required control performance, when there are variations in the plant parameters and operating conditions. Therefore, to insure that the controller can deal with the variations in the

plant a tuning process must be performed. The most famous, which is frequently used in industrial applications to tune the PID controller is the Ziegler-Nichols(ZN) method which does not require a system model and control parameters are designed from the plant step response. Tuning using this method is characterized by a good disturbance rejection but on the other hand, the step response has a large percentage overshoot in addition to a high control signal that is required for the adequate performance of the system. The model based techniques such as frequency response methods, Root locus and pole assignment design techniques are also proposed in addition to transient response specifications. The efficiency of the tuning law depends on the accuracy of the proposed model as well as the assumed conditions with respect to actual operating conditions.

Artificial Intelligence (AI) techniques such as neural networks, fuzzy logic and genetic algorithms are gaining increased interest nowadays. A lot of techniques have been proposed to tune the gains of PI controller based on AI techniques: Self tuning FL and neural network techniques, GA based online and offline[3] tuning procedures are some of these methods proposed for the online adaptive tuning of PI controller. In such application, the controller gains are tuned with the variation of system conditions. The advantage of these techniques is that they are model free strategies because they use the human experience for the generation of the tuning law. This paper provides a comparison between two strategies (FSM1, FSM2) used for tuning the PI speed controller in the direct torque controlled induction motor.

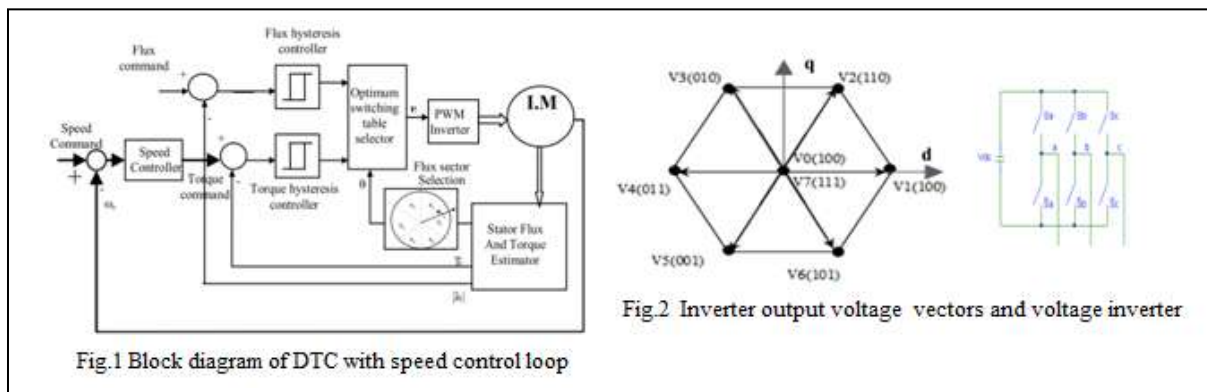
## II DIRECT TORQUE CONTROL

In principle, DTC is a direct hysteresis stator flux and electromagnetic torque control which triggers one of the eight available discrete space voltage vectors generated by a Voltage Source Inverter (VSI) in order to keep stator flux and motor The inverter Voltage vectors shown in Fig. 2. The selection is made in order to maintain torque and flux error inside the hysteresis band in which the errors are indicated by  $\Delta T_e$  and  $\Delta \Psi_s^s$  respectively.

$$\Delta T_e = T_{seff} - \dots(1)$$

$$\Delta \Psi_s^s = \bar{\Psi}_{seff}^s - \dots(2)$$

The six different directions of noted as (i=1 to 6). Considering , and as the combination of switches status of the inverter are given by the expression(3).[4][5]



$$\bar{V}_s^s = \frac{2}{3} V_{dc} \left[ S_a + S_b \exp \left( j \frac{2\pi}{3} \right) + S_c \exp \left( j \frac{4\pi}{3} \right) \right] \text{---(3)}$$

### 2.1 Stator Flux Control

By selecting the appropriate inverter output voltage  $\bar{V}_i$ , the stator flux  $\Psi_s^s$  rotates at the desired frequency  $\omega_s$  inside a specified band.

$$\bar{\Psi}_s^s = \int \left( \bar{V}_s^s - \bar{i}_s^s R_s \right) dt \text{---(4)}$$

Where  $\bar{V}_s^s$  and  $\bar{i}_s^s$  indicate the measured stator voltage and current respectively. If the stator ohmic drops are neglected,

$$\bar{\Psi}_s^s = \int \bar{V}_s^s dt \text{---(5)}$$

Therefore the variation of the stator flux space vector due to the application of the stator voltage vector during a time interval of  $\Delta t$  can be approximated as:[4][5][6]

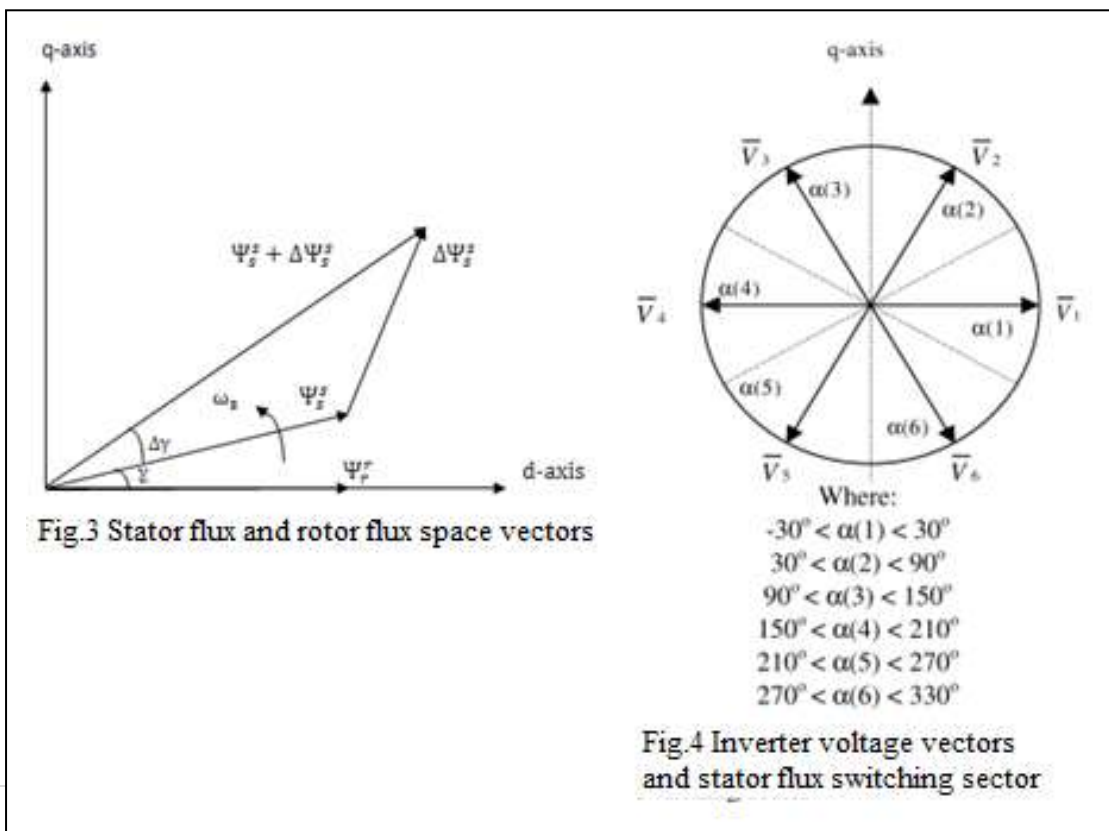
$$\Delta \Psi_s^s = \bar{V}_i \Delta t \text{---(6)}$$

### 2.2 Torque Control

The electromagnetic torque given by equation (7) is a sinusoidal function of  $\gamma$  the angle between  $\bar{\Psi}_s^s$  and  $\bar{\Psi}_r^r$  as shown in Fig. 3. Since the rotor flux changes slowly, the rapid variation of stator flux space vector will produce a variation in the developed torque because of the variation of the angle  $\gamma$  between the two vectors:

$$T = \frac{3}{2} P \bar{\Psi}_s^s \cdot \bar{\Psi}_r^r \sin \gamma \text{---(7)}$$

$$\Delta T_e = \frac{3}{2} \cdot \frac{P}{2} \frac{L_m}{L_s L_r - L_m^2} \left[ (\Psi_s^s + \Delta \Psi_s^s) \cdot \Psi_r^r \right] \sin \gamma \text{---(8)}$$



Therefore to obtain a good dynamic performance, an appropriate inverter voltage vectors has to be selected to obtain stronger rotation speed of  $\omega_s$  [4][5][7] .

The actual value of stator flux can be expressed as:

$$\bar{\Psi}_s^s = \int (\bar{V}_s^s - \bar{i}_s^s R_s) dt \quad \text{-----(9)}$$

The electromagnetic torque is calculated by means of equation (10)

$$T_e = \frac{3}{2} \cdot P \cdot (\Psi_{ds}^s i_{qs}^s - \Psi_{qs}^s i_{ds}^s) \quad \text{----- (10)}$$

dψ	dT <sub>e</sub>	α(1) sector	α(2) sector	α(3) sector	α(4) sector	α(5) sector	α(6) sector
		1	2	3	4	5	6
1	1	$\bar{V}_2$	$\bar{V}_3$	$\bar{V}_4$	$\bar{V}_5$	$\bar{V}_6$	$\bar{V}_1$
	0	$\bar{V}_7$	$\bar{V}_0$	$\bar{V}_7$	$\bar{V}_0$	$\bar{V}_7$	$\bar{V}_0$
	-1	$\bar{V}_6$	$\bar{V}_1$	$\bar{V}_2$	$\bar{V}_3$	$\bar{V}_4$	$\bar{V}_5$
0	1	$\bar{V}_3$	$\bar{V}_4$	$\bar{V}_5$	$\bar{V}_6$	$\bar{V}_1$	$\bar{V}_2$
	0	$\bar{V}_0$	$\bar{V}_7$	$\bar{V}_0$	$\bar{V}_7$	$\bar{V}_0$	$\bar{V}_7$
	-1	$\bar{V}_5$	$\bar{V}_6$	$\bar{V}_1$	$\bar{V}_2$	$\bar{V}_3$	$\bar{V}_4$

Table 1: Switching table of inverter voltage vectors

### 2.3 Inverter optimal Switching Table

On the basis of the torque and flux hysteresis status and of the stator flux switching sector, which is denoted by  $\alpha$ , DTC algorithm selects the inverter voltage vector to apply to the induction machine from the Table 1. The outputs of the switching table are the settings for the switching devices of the inverter. Figure 4 shows the relation of inverter voltage vector and the stator flux switching sectors.

$$\alpha = \angle \bar{\Psi}_s^s = \tan^{-1} \left( \frac{q}{p} \right) \quad \text{----(11)}$$

Active switching vectors are  $\bar{V}_1(1); \bar{V}_2(1); \bar{V}_3(0); \bar{V}_4(0); \bar{V}_5(0); \bar{V}_6(1)$

Zero switching vectors are  $\bar{V}_0(0); \bar{V}_7(0); [8]$

### III SLIDING MODE CONTROLLER (SMC)

Sliding mode controller is suitable for a specific class of nonlinear systems. This is applied in the presence of modeling inaccuracies, parameter variation and disturbances, provided that the upper bounds of their absolute values are known. Modeling inaccuracies may come from certain uncertainty about the plant (e.g. unknown plant parameters), or from the choice of a simplified representation of the system dynamic. Sliding mode controller design provides a systematic approach to the problem of maintaining stability and satisfactory performance in presence of modeling imperfections [9].

SMC is known for its capability to cope with bounded disturbance as well as model imprecision which makes it ideal for the robust nonlinear control of induction motor drives .To design a sliding mode speed controller for the induction motor DTC drive, consider the mechanical equation:

$$\frac{J}{P} \dot{\omega} + \frac{B}{P} \omega + T_L = T \quad \text{----- (12)}$$

Where  $\omega$  is the rotor speed in electrical rad/s, rearranging to get:

$$\dot{\omega} = -\frac{B}{J}\omega - \frac{P}{J}T_L + \frac{P}{J}T_e \quad \text{---- (13)}$$

Considering  $\Delta a$  and  $\Delta b$  as bounded uncertainties introduced by system parameters J and B, the equation(13) can be rewritten as [10]:

$$\dot{\omega} = (a + \Delta a)\omega + (b + \Delta b)T_e + cT_L \quad \text{---- (14)}$$

Where  $a = -\frac{B}{J}, b = \frac{P}{J}, c = -\frac{P}{J}$

Defining the state variable of the speed error as:

$$e(t) = \omega(t) - \omega^*(t) \quad \text{--- (15)}$$

$$\frac{d}{dt}e(t) = \dot{e}(t) \quad \text{---- (16)}$$

Combining equations (14), (15)

$$\dot{e}(t) = ae(t) + b[\bar{T}_e + d(t)] \quad \text{---- (17)}$$

Where  $\bar{T}_e = T_e + \frac{a}{b}\omega^*, d(t) = \frac{\Delta a}{b}\omega + \frac{\Delta b}{b}T_e + \frac{c}{b}T_L$  ---- (18)

Defining a sliding surface  $s(t)$  from the nominal values of system parameters a and b [10][11]

$$s(t) = e(t) - \int_0^t (a + bk)e(\tau) d\tau \quad \text{---- (19)}$$

Such that the error dynamics at the sliding surface  $s(t) = s'(t) = 0$  will be forced to exponentially decay to zero, then the error dynamics can be described by:

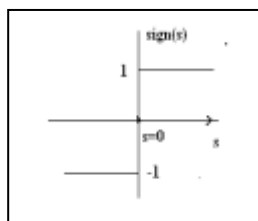
$$\dot{e}(t) = (a + bk)e(t) \quad \text{----(20)}$$

Where k is a linear negative feedback gain .

Variable structure speed controller  $= ke(t) - \beta \text{sgn}(s)$  ---(21)

Where  $\beta$  is known as hitting control gain used to make the sliding mode condition possible and the sign function can be defined as

$$\text{Sign}(s) = \begin{cases} 1 & \text{if } s > 0 \\ 0 & \text{if } s = 0 \\ -1 & \text{if } s < 0 \end{cases} \quad \text{----(22)}$$



To guarantee the existence of the switching surface consider the Lyapunov function [12]. Based on Lyapunov Theory, if the function  $\dot{v}(t)$  is negative definite, this will ensure that system trajectory will be driven and attracted towards the sliding surface  $s(t)$  and once reached, it will remain sliding on it until the origin is reached asymptotically[12].

$$v(t) = \frac{1}{2} s^2 \quad \text{---(23)}$$

Taking the derivative of equation (23) and substituting the equation (19)

$$\dot{v}(t) = s(t) \cdot \dot{s}(t) = s(t) \cdot \{e(t) - (a + bk)e(t)\} \quad \text{---(24)}$$

Using the equations (17), (21)  $\dot{v}(t) = s(t) \cdot \{-b(\beta \text{sign}(s)) - d(t)\} \quad \text{--- (25)}$

To ensure the equation (25) always negative definite, the value of hitting control gain  $\beta$  should be designed as the upper bound of the lumped uncertainties  $d(t)$  i.e  $\beta \geq |d(t)|$

The hitting control gain  $\beta$  has to be chosen large enough to overcome the effect of any external disturbance [12][13]. Therefore the speed control law defined in will guarantee the existence of the switching surface  $s(t)$  in and when the error function  $e(t)$  reaches the sliding surface, the system dynamics will be governed by which is always stable [10]. Moreover, the control system will be insensitive to the uncertainties  $\Delta a$ ,  $\Delta b$  and the load  $T_L$ .

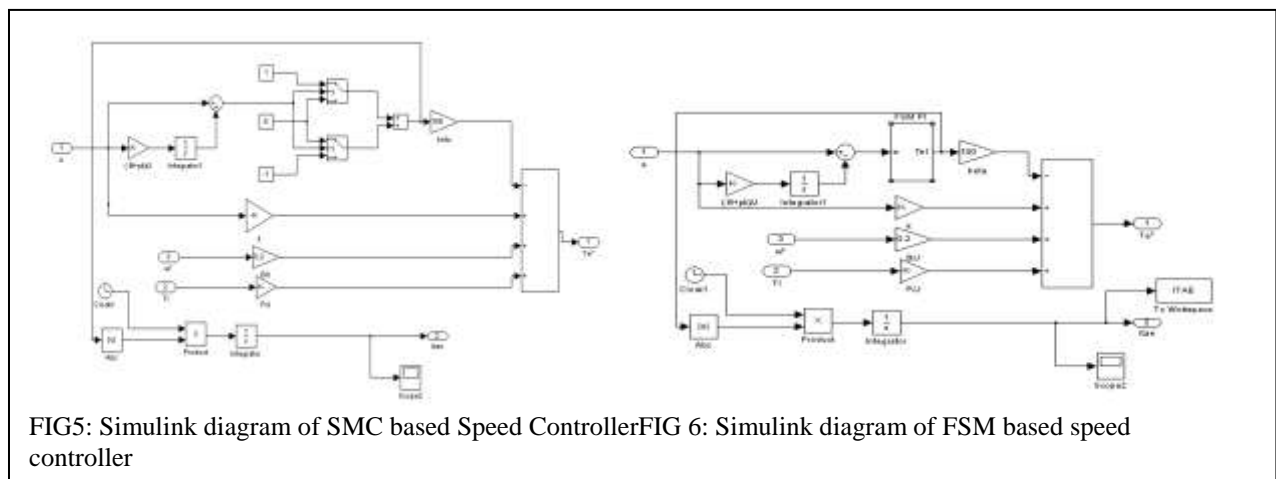


FIG5: Simulink diagram of SMC based Speed Controller FIG 6: Simulink diagram of FSM based speed controller

**IV FUZZY BASED SLIDING MODE CONTROLLER**

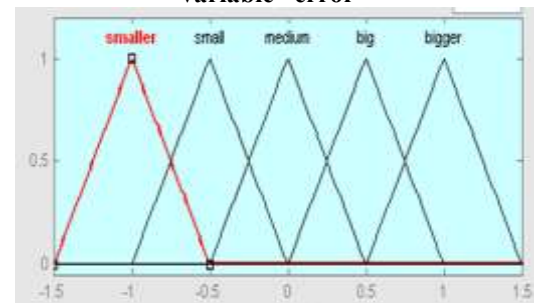
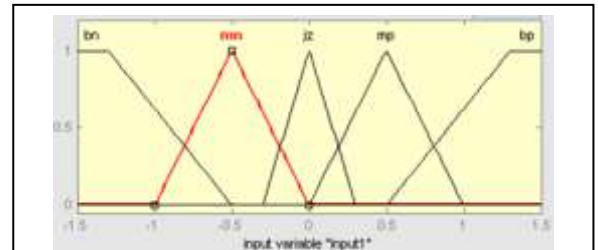
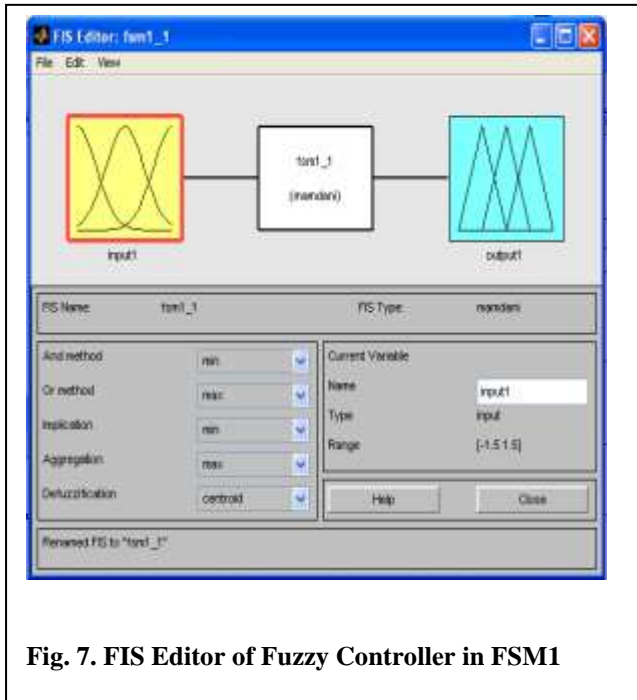
The sign function in the sliding mode control will cause high frequency chattering due to the discontinuous control action which represents a severe problem when the system state is close to the sliding surface [6]. To overcome this problem a boundary layer  $\Phi$  is introduced around the switching surface and the sign function will be replaced by a saturation function  $\text{sat}(s / \Phi)$  [6]. The choice of  $\Phi$  is crucial; small values of  $\Phi$  may not solve the chattering problem and large values may increase the steady state error, requiring a compromise choice when selecting the boundary layer thickness.

To reduce the chattering phenomenon is to combine FL with a SMC [6]. Hence two new Fuzzy Sliding Mode (FSM) controllers are formed with the robustness of SMC and the smoothness of FL. The switching functions of

sliding mode and FSM schemes are shown in Figures5,6. In this technique the saturation function is replaced by a fuzzy inference system to smooth the control action.

#### 4.1 FSM1

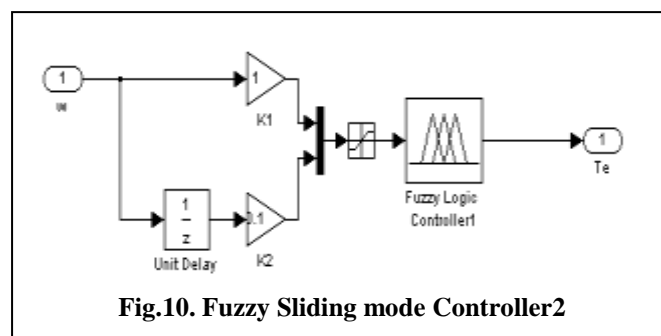
The fuzzy sliding mode controller1 is shown in Fig. 7 to Fig.9.



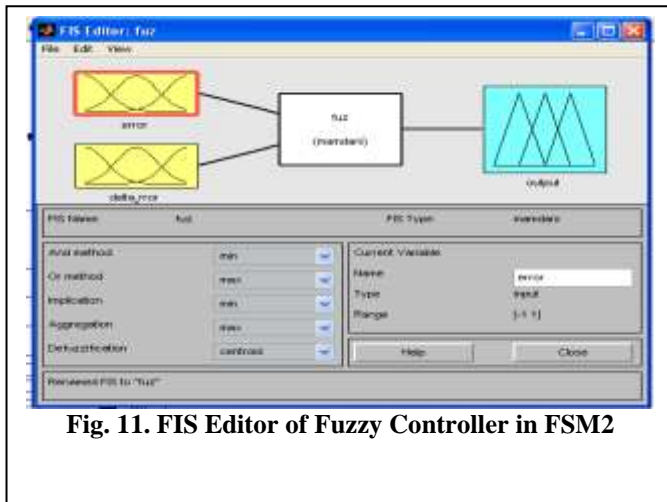
**Table2:Fuzzy rules for FSM1**

Input(e)	bn	mn	jz	mp	bp
output	bigger	big	medium	small	smaller

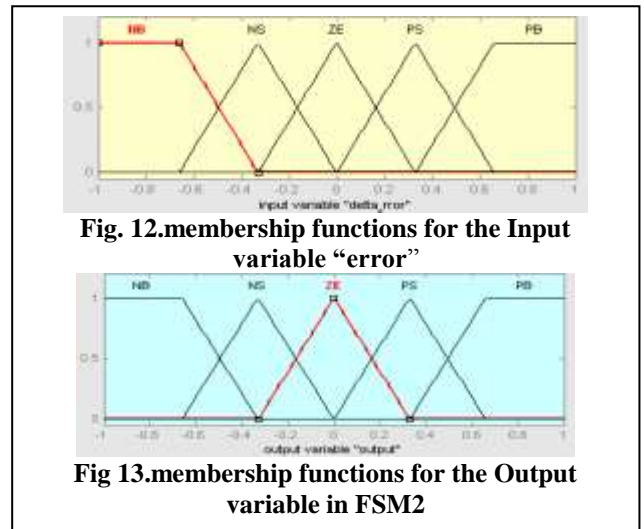
#### 4.2 FSM2



The inputs given to the FSM2 are two and are shown in the fig10[14]. the matlab models of fuzzy controllers are shown in the figures11 to 13. The membership functions for the first input “error” is same as in FSM1. The fuzzy rules are taken trial and error to get the optimized response. Fuzzy rules are shown in the table3.



**Fig. 11. FIS Editor of Fuzzy Controller in FSM2**



**Fig. 12. membership functions for the Input variable “error”**

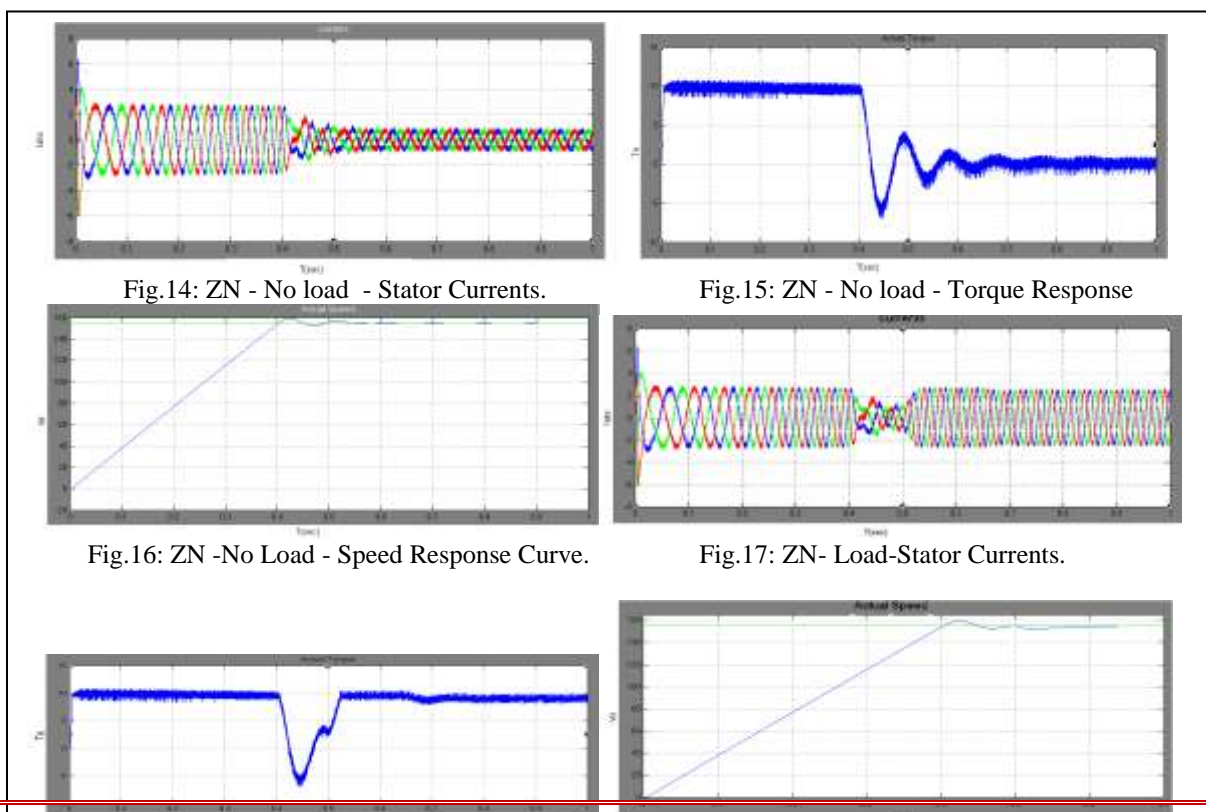
**Fig 13. membership functions for the Output variable in FSM2**

The membership functions for the input fuzzy set error , output is same as in FSM1. Where as the membership functions for the second input is shown in the figure 12.

**Table3: Fuzzy Rules for FSM2**

e/de	NB	NS	ZE	PS	PB
NB	ZE	PS	PB	PS	ZE
NS	NS	ZE	PS	ZE	NS
ZE	NB	NS	ZE	NS	NB
PS	NS	ZE	PS	ZE	NS
PB	ZE	PS	PB	PS	ZE

**V RESULTS**



**Fig.14: ZN - No load - Stator Currents.**

**Fig.15: ZN - No load - Torque Response**

**Fig.16: ZN -No Load - Speed Response Curve.**

**Fig.17: ZN- Load-Stator Currents.**

**Fig.18: ZN - Load-Torque Response**

**Fig.19: ZN - Load - Speed Response Curve.**



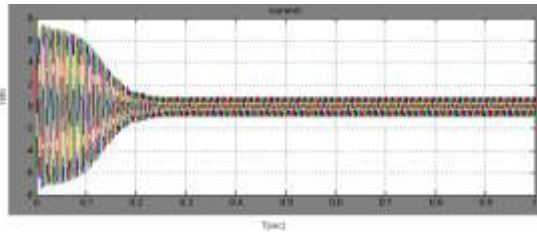


Fig.20: FSM1- No load - Stator Currents.

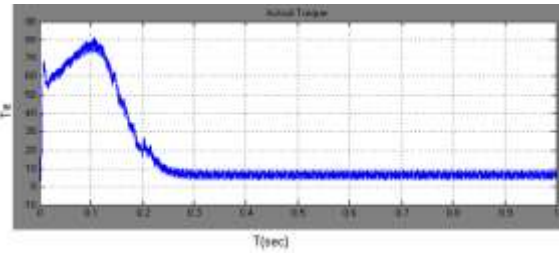


Fig.21: FSM1 - No load - Torque Response

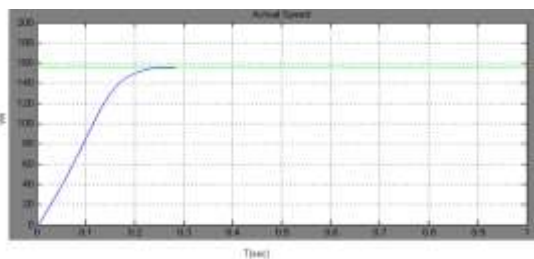


Fig.22: FSM1 -No load - Speed Response Curve

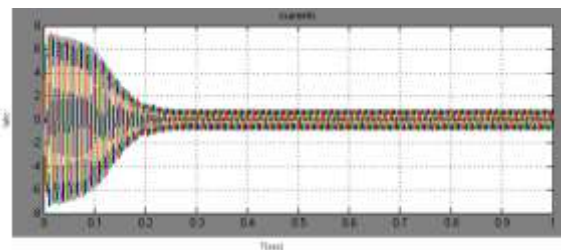


Fig.23: FSM1- Load - Stator Currents.

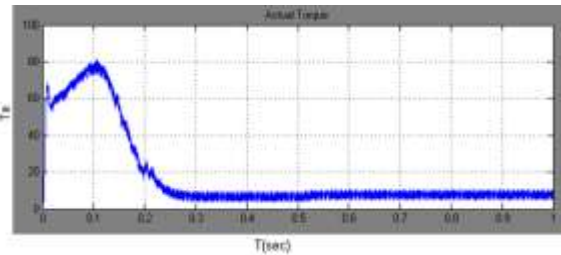


Fig.24: FSM1- Load - Torque Response.

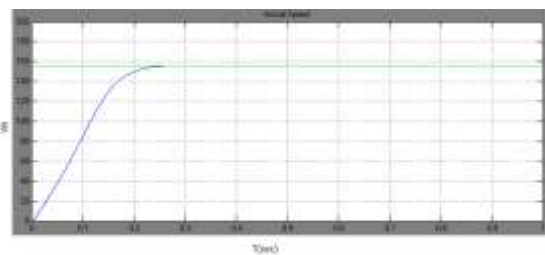


Fig.25: FSM1 - Load - Speed Response Curve

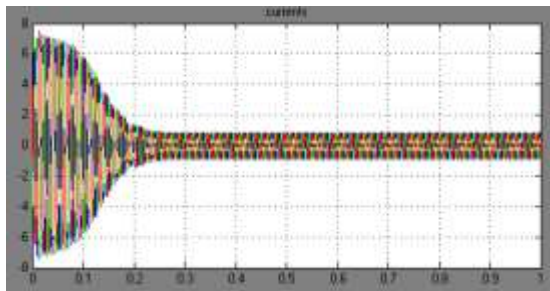


Fig.26.: FSM2- no Load - Stator Currents.

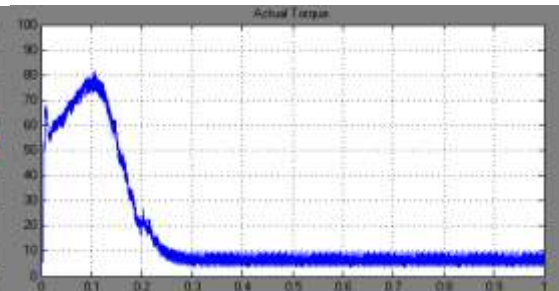


Fig.27: FSM2 - no Load - Torque Response.

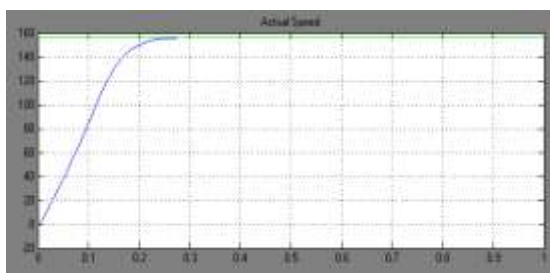


Fig.28: FSM2 – no Load - Speed Response Curve

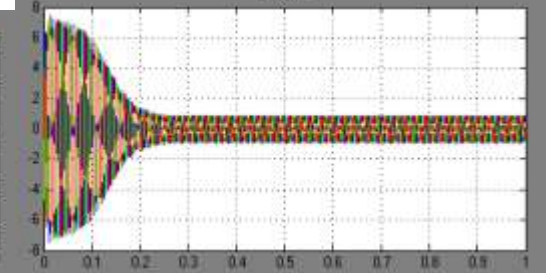
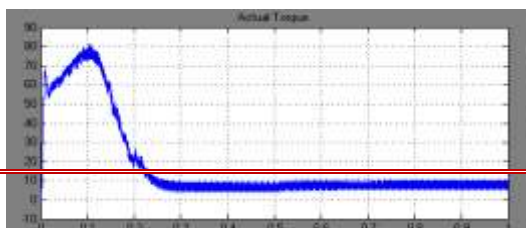


Fig.29: FSM2- Load - Stator Currents.



Compared the speed controllers of ZN, SMC, and FSM based methods. The figures 14 to 31 shows the stator currents, torque, speed response curves of ZN,FSM1,FSM2 based controllers without load and with step change in load  $T=9\text{N-m}$  applied at 0.5 seconds .

Response Specifications	Ziegler-Nichols method $K_p=0.612,$ $k_i=122.4$	SMC	FSM1	FSM2
ITAE	4.46	0.5	0.49	0.3718
Speed response settling time in sec	0.44	0.25	0.22	0.2
Transient response	2.77% overshoot	No overshoot	No overshoot	No overshoot
Response to load torque application (load torque 9N-m is applied at 0.5 sec)	Speed drops to 152 rad/sec from 155 rad/sec	Speed drops to 156 rad/sec from 157 rad/sec	Speed drops to 155.5 rad/sec from 156 rad/sec then quickly regained the reference speed	Speed drops to 155.5 rad/sec from 156 rad/sec then quickly regained the reference speed

**Table4: comparison of results of ZN, SMC, FSM1, FSM2 controllers.**

## VI CONCLUSION

Simulation has been carried out for ZN, SMC, FSM1 and FSM2 controllers with no load and load of 9N-m applied at 0.5 sec, The results are tabulated in the table4. The controller coefficients used in FSM are  $k=-2.3e-4$ ,  $\beta=100$ [7]. ITAE is very less in FSM1 FSM2 based controllers.FSM2 has less ITAE and reached steady state in 0.2 seconds. And there was no overshoot in both SMC, FSM1,FSM2 bases controllers

## MOTOR PARAMETERS

$P=4$ ,  $R_s=7.83\Omega$ ,  $R_r=7.55\Omega$ ,  $L_s=L_r=0.4751\text{H}$ ,  $L_m=0.4535\text{H}$ ,  $V_{dc}=400\text{V}$ ,  $J=0.03\text{kg/m}^3$ ,  $B=0.006$ ,  $P=1.5\text{Kw}$ ,  $T_L=9\text{N-m}$ ,  $N_{\text{RATED}}=1480\text{rpm}(155\text{rad/sec})$

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