

# FESA: FUZZY CONTROLLED ENERGY EFFICIENT SELECTIVE ALLOCATION AND REALLOCATION OF TASKS AMONG MOBILE ROBOTS

**Dr. Anuradha Banerjee**

*Dept of Computer Applications, Kalyani Govt. Engg. College, West Bengal.(India)*

## ABSTRACT

*Energy aware operation is one of the visionary goals in the area of robotics because operability of robots is greatly dependent upon their residual energy. Practically, the tasks allocated to robots carry different priority and often an upper limit of timestamp is imposed within which the task needs to be completed. If a robot is unable to complete one particular task given to it the task is reallocated to some other robot. The collection of robots is controlled by a Central Monitoring Unit (CMU). Selection of the new robot is performed by a fuzzy controller called Task Reallocator (TRAC). It accepts the parameters like residual energy of robots, possibility that the task will be successfully completed by the new robot within stipulated time, distance of the new robot (where the task is reallocated) from distance of the old one (where the task was going on) etc. The proposed methodology increases the probability of completing globally assigned tasks and saves huge amount of energy as far as the collection of robots is concerned.*

**Keywords:** *Energy efficiency, Fuzzy Controller, Priority, Selection, Task.*

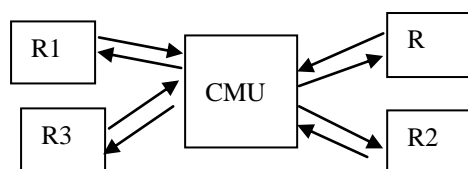
## I. INTRODUCTION

The present article focuses on the efficient distribution of tasks among a collection of mobile robots, which are centrally controlled by a Central Monitoring Unit (CMU). All robots can directly send signals to CMU and receive signals from it. The situation can be detected from figure 1 where R, R1, R2 and R3 are the robots. CMU keeps track of the residual energy of robots, tasks that are allocated to them and the present status of execution of those tasks along with the constraints associated with them. A decision process is initiated in order to accept/ reject tasks for further processing as well as to continue/ re-allocate a task in progress. On a global point of view, a task allocation procedure is initiated after arrival of a new job or cancellation of an ongoing task subjected to the availability of able robots.

Studies on energy-aware operation and task allocation among mobile robots are in progress in a number of research groups. F. Dressler and G. Fuchs [1] proposed an energy-aware task allocation among mobile robots where only the residual energy of robots are considered. Issues of coordination among mobile robots are presented in [2] and [3] whereas cooperation issues are discussed in [4]. One of the most commonly used task allocation strategies in robotics are threshold based systems. These systems are based on observations of task or role allocation processes in social insects, whereby tasks, often implicitly, send out a signal, and the insects/robots react to this signal if it surpasses an internal threshold. Due to differences in this threshold among individuals, task allocation emerges in proportion to the task's signal intensity [7]. In [6], a variation of this

mechanism is presented whereby all robots have the same threshold and the differentiation comes from the variability in the local observation of the signal intensity by the individuals. In [8] an ant-like task allocation model was proposed that is based on local threshold value for energy efficiency.

The rest of the paper is organized as follows. Section 2 illustrates the basic system model. Heuristics that drive TRAC are discussed in section 3. Design of TRAC is performed in section 4. Section 5 emphasizes the effectiveness of our proposed scheme through extensive simulation results. Section 6 analyzes the complexity of our proposed scheme FESA and section 7 concludes the paper.



**Fig.1 Signal transmission and reception between CMU and robots R, R1, R2 and R3**

### 1.1 System Model of FESA

The system of FESA consists of a collection of robots and a CMU that allocates and reallocates the tasks to robots as the tasks arrive into the system. The system is non-preemptive. Once a task is allocated to a robot, say R1, it is allowed to continue its task till the upper limit of time duration associated with the task elapses or some unnatural incident makes R1 unable to operate any further. For example, fire may break out into the system and destroy R1. It may be noted that, at any point of time a task may be allocated to exactly one robot. When a new task arrives into the system it is initially allocated to any idle robot possessing sufficient amount of energy to complete the task. If no such robot is found, then the task is allocated to one of the robots having maximum residual energy. The intention is to complete a task as much as possible. On the other hand, during reallocation, CMU consults the TRAC embedded in it to find the best possible robot to carry out the pending task. A task is reallocated if sufficient time is there to complete the task i.e. upper limit of timestamp within which the task needs to be completed, is not crossed, at least one operational idle robot is there and no task with higher priority is waiting at that time for being allocated or reallocated to robots. CMU maintains three different tables termed as ROBOT\_TABLE, TASK\_TABLE and HISTORY\_TABLE. CMU also stores the maximum possible distance between any two robots through a path traversable in the present geographical scenario. Attributes of the mentioned tables are shown below:

ROBOT_TABLE
Robot_id
Enrg_tot
Enrg_thres

HISTORY_TABLE
Robot_id
Task_id
Task_portion
Session_id
Assign_timestamp
Release_timestamp

TASK_TABLE
Task_id
Priority
Completion_timestamp

Ptr_robotarray
Enrg_task
Enrg_rem_task
Status

A tuple (p,q,r) in the ROBOT\_TABLE indicates that p is identification number of one robot, q is its total energy and r is its energy threshold. According to the characteristic curve of the batteries used in mobile robots, voltage drop shows a linear decline until some critical value [1, 2]. After that point the voltage drop speeds up quickly with very small remaining time left for execution [1]. Energy of the robot corresponding to the critical voltage is termed as energy threshold of the robot.

A tuple (p, ts, tp, sid, atm, rtm) in the HISTORY\_TABLE signifies that the robot p completed tp portion of the task ts within time interval (rtm-atm) in session sid. atm is the timestamp at which the task was assigned and rtm is the time at which the task finished. Similarly, a tuple (ts, pr, ct, rbr, et, etrem, st) in TASK\_TABLE denotes that the task with identification number ts has priority pr and it needs to be completed within timestamp ct. rbr is pointer to a list. Each entry of the list contains identification numbers of the robots to which the task was assigned earlier, portion of the task that was assigned along with the corresponding timestamp, the timestamp when the robot unsuccessfully stopped execution of that portion of the task and portion of the task remaining to be executed. et is the minimum energy required to accomplish the whole task whereas etrem is the minimum energy required to accomplish the remaining portion of the task. All possible values of st are 0 and 1. It is set to 0 if the task is being executed and set to 1 if it cannot be completed (possible reasons are unavailability of robots, completion time constraints etc.).

During reallocation, portion of a task may be reallocated. For example, let 50% of a task has been carried out by a robot R1 after which it suddenly stopped operating. Then the rest 50% of the same work can be allocated to some other robot R2 although it is not possible in our proposed scheme to allocate 30% of the remaining task to R2 and the rest to R3, simultaneously. At any point of time, one particular task cannot run in more than one robot, even partly.

## 1.2 Heuristics of TRAC

The fuzzy controller TRAC, which is responsible for task reallocation, performs according to the following heuristics:

- i) If a robot R is equipped with high residual battery power so that the residual energy above its energy threshold is greater than the energy required to accomplish the remaining portion of task A, then R is in an advantageous position to execute that portion of the task.
- ii) According to the HISTORY\_TABLE of CMU, if a robot R has successfully accomplished the task A earlier within the mentioned stipulated time duration, then R has a good chance of being assigned the same task A in future.
- iii) If the minimum geographical distance through a traversable region within the given scenario, of the old robot R1 (where a task A was going on earlier) from the new robot R (where A is going to be reallocated) is small, then it will be beneficial for the new robot R to resume the task, specially when the task is of the type exploration and supervision of unknown surroundings.
- iv) If a robot R has got a bad failure history i.e. failed to complete a number of tasks on so many

occasions, then it is better to avoid R during reallocation of tasks.

The observations expressed above are in the form of if-then rules which are the basic unit of fuzzy function approximation. Advantages of fuzzy logic are that it is flexible, conceptually easy to understand and based on natural language. Moreover, it is tolerant of imprecise data and can model non-linear functions of arbitrary complexity. All these encouraged us to design the scheme of FESA using fuzzy logic.

## II. DESIGN OF TRAC

### 2.1 Formulation of parameters

The input parameters of TRAC are energy\_efficiency, history\_of\_support, distance\_quotient and failure\_quotient. These are formulated below based on the assumption that the current timestamp is t and TRAC is considering to reallocate a portion  $\rho(A,t)$  of task A in robot R. R1 is the old robot where the task A was being carried out.

#### *Energy\_efficiency*

The energy\_efficiency  $\alpha_R(t)$  of a robot R at time t is given by,

$$\alpha_R(t) = 1 - e_A / (E_R(t) - \text{Ethres}_R) \quad (1)$$

$e_A$  specifies the minimum energy required to complete portion of the task A to be reallocated.  $E_R(t)$  is the residual energy of robot R at time t and  $\text{Ethres}_R$  signifies the threshold energy of the same robot. It is quite evident from (1) that  $\alpha_R(t)$  lies between  $-\infty$  and 1. Positive fractional values of  $\alpha_R(t)$  puts R in a good position to carry out the task  $\rho(A,t)$ .

#### *History\_of\_support*

Let  $H(R,A)$  denote the set of occasions or sessions during which the robot R successfully completed execution of the portion of task A that was given to it abiding by the time constraint associated with the task. Also assume that  $HF(R,A)$  denote the set of occasions or sessions during which the robot R could not successfully complete execution of the portion of task A that was given to it. Then, history\_of\_support  $h_{R,A}(t)$  of robot R at time t with respect to task A is given by,

$$h_{R,A}(t) = \begin{cases} (h'_{R,A}(t) / T\_C(A)) & \text{if } (h'_{R,A}(t) / T\_C(A)) \geq 1 \\ (h'_{R,A}(t) / T\_C(A)) \exp Z(R,A) & \text{otherwise} \end{cases} \quad (2)$$

$$h'_{R,A}(t) = \left[ \left\{ t + \prod_{w \in H(R,A)} (\beta_{R,w} / q_w(A)) \right\}^{1/H(R,A)} \right] \times \rho(A,t) \quad (3)$$

$$Z(R,A) = H(R,A) / \{H(R,A) + HF(R,A)\}$$

According to the history of behavior of robot R, in session w,  $q_w(A)$  portion of the task A has been completed by robot R in time duration  $\beta_{R,w}$ .  $T\_C(A)$  is the timestamp within which the task A must be fully completed. If  $h_{R,A}(t)$  is less than 1 then R has a good chance to be assigned the task  $\rho(A,t)$ .  $h_{R,A}(t)$  should acquire a low value

if number of successes of robot R with respect to task A is high and number of failures of R with respect to task A is low, i.e. if  $H(R,A)$  is high and  $HF(R,A)$ . This is correctly modeled through  $Z(R,A)$ .

### ***Distance\_quotient***

Let  $dist_{R,R1}(t)$  be the least geographical distance between the robots R1 and R at time t through a path which is traversable in the present scenario. Also assume that  $dist\_max$  is the maximum possible distance between any two robots through a path traversable in the present scenario. Then, the distance\_quotient  $dq_{R,R1}(t)$  of robot R w.r.t. robot R1 at time t is given by,

$$dq_{R,R1}(t) = dist_{R,R1}(t) / dist\_max \quad (4)$$

Distance\_quotient lies between 0 and 1. Values close to 0 indicate that R won't have to make huge extra efforts to resume the pending task A of R1.

### ***Failure\_quotient***

Let  $\beta_R(t)$  be the number of tasks allocated to robot R within time t, irrespective of whether they were allocated fully or partly. Among them, on  $\beta'_R(t)$  number of occasions the tasks had to be reallocated from R. Hence, the failure quotient  $fq_R(t)$  of robot R at time t based on the history of it's behavior, is,

$$fq_R(t) = \beta'_R(t) / \beta_R(t) \quad (5)$$

Actually failure quotient of a robot indicates its general attitude towards the tasks assigned to it by the CMU. If it is high then it denotes that R is only eager to relinquish its tasks. Please note that  $fq$  also ranges between 0 and 1.

## **2.2 Rule Bases of TRAC**

As far as the range division of  $\alpha$  is concerned, the range from  $-\infty$  to 0 is not advantageous for the system and it is denoted as a1. The ranges from 0-0.33, 0.33-0.66, 0.66-1 are indicated as a2, a3 and a4 respectively. For range division of h, the ranges from 0-0.33, 0.33-0.66, 0.66-1 are indicated as a1, a2 and a3 respectively. The range from  $1-\infty$  is not acceptable and it is denoted as a4. For the subsequent two parameters  $dq$  and  $fq$  the range division is uniform between 0 and 1, i.e. 0-0.25 is a1, 0.25-0.50 is a2, 0.50-0.75 is a3 and 0.75-1 as a4. Please note that the subscripts have been omitted here for simplicity.

Table 1 shows the fuzzy composition of energy efficiency and history\_of\_support generating a temporary output t1. History\_of\_support plays a significant role in determining whether a pending task will be reallocated to one particular robot only if energy of the robot is sufficiently high to accomplish that task. t1 is combined with failure quotient in table 2 generating another temporary output t2. t1 dominates in table 2 because it is a combination of two parameters which are equally or more important than  $fq$ . Similarly, t2 is combined with  $dq$  in table 3 generating the ultimate output reloc. Here also t2 dominates for the reasons described earlier in case of table 2.

Table.1. Fuzzy Combination of  $\alpha$  and h Generating t1

$\alpha \rightarrow$	a1	a2	a3	a4
h $\downarrow$				
a1	a1	a2	a3	a4
a2	a1	a2	a3	a4
a3	a1	a2	a2	a3
a4	a1	a1	a1	a2

Table.2. Fuzzy Combination of t1 and fq Generating t2

t1 $\rightarrow$	a1	a2	a3	a4
fq $\downarrow$				
a1	a1	a2	a3	a4
a2	a1	a2	a3	a4
a3	a1	a2	a3	a3
a4	a1	a1	a2	a3

Table.3. Fuzzy Combination of t2 and dq Generating reloc

t2 $\rightarrow$	a1	a2	a3	a4
dq $\downarrow$				
a1	a1	a2	a3	a4
a2	a1	a2	a3	a4
a3	a1	a2	a3	a4
a4	a1	a2	a2	a3

Among the various value ranges of reloc of different robots, any one possessing the highest value range will be selected for reallocation of a certain job.

### III. SIMULATION RESULTS

For simulation, I have used the Webots 3D physics-based robotics simulator [9] to create the virtual world which the robots mapped and navigated as part of the experiments. Webots has high fidelity and models realistic sensor and motion errors. In the simulation experiments I used RV-400 [10] robots. In various runs, the number of robots was 3, 6, 9, 11 and 14 while the number of tasks was 5, 9, 12, 15 and 20. The tasks are to explore portions of a room of different sizes. The simulation was carried out for approximately 3000 seconds. The results reported graphically in this section correspond to the average of all the simulation runs.

Performance of the present scheme has been compared with other state-of-the-art techniques that address the similar issue i.e. energy-aware operation and task allocation (EOTA [1]) and ant-like task allocation (ATA [8]) models. Performance matrices are consumed energy per robot, percentage of successfully completed tasks, delay for completion of each task and required percentage of reallocation. The results reveal that our proposed scheme *Fuzzy-controlled Energy-efficient Selective Allocation* (FESA) outperforms its competitors in every respect. The results are graphically shown in figures 2, 3, 4 and 5.

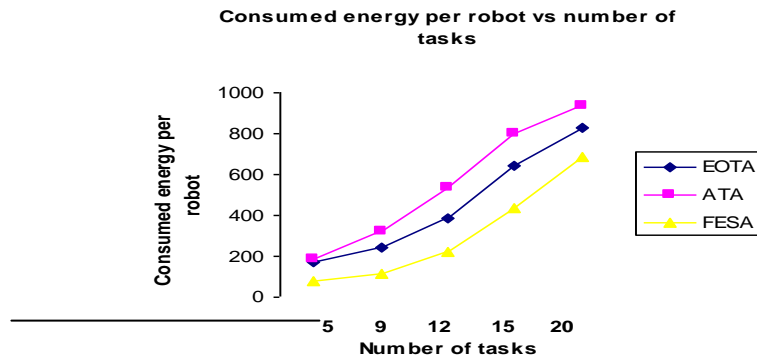


Figure 2: Graphical illustration of consumed energy in Joule per robot vs number of tasks

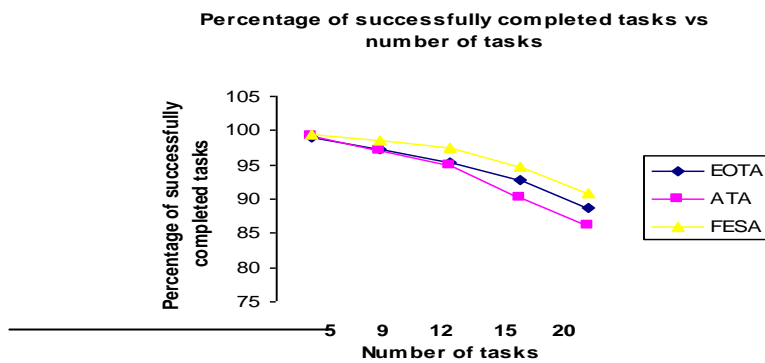


Figure 3: Graphical illustration of percentage of successfully completed tasks vs number of tasks

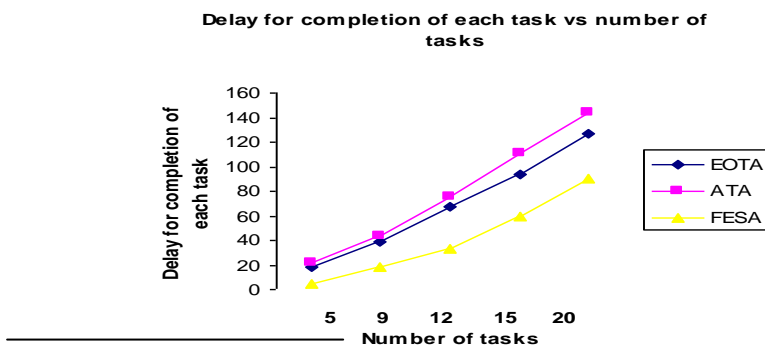


Figure 4: Graphical illustration of delay for completion of each task in seconds vs number of tasks

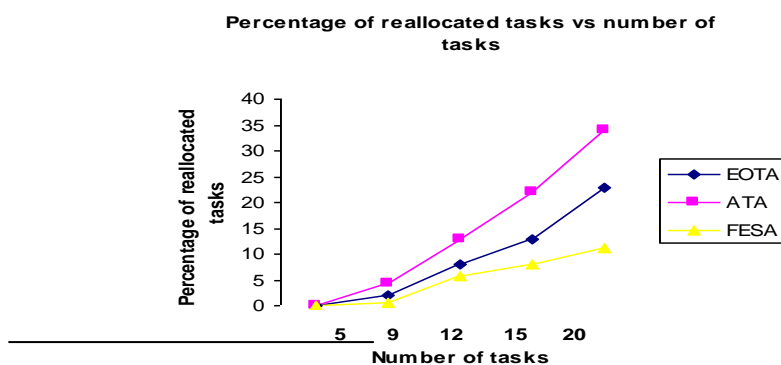


Figure 5: Graphical illustration of percentage of reallocated tasks vs number of tasks

If a robot is bound to execute some task when its residual energy is less than energy threshold, then its rate of energy consumption abruptly increases. Our proposed scheme FESA always tries to allocate or reallocate tasks to those robots that have sufficient battery power to execute the tasks. Moreover, during reallocation, FESA tries to find new robots which are geographically close to the old one so that the new robot chosen by TRAC can efficiently take over the charge of the old one without much effort. This is particularly useful for the tasks like exploring a room. All these contribute to the reduction of energy consumption in favor of our proposed scheme FESA. However, it is quite trivial that the amount of energy consumption for each robot will increase for all the task allocation schemes as the number of tasks increase. This is illustrated in figure 2.

By analyzing the attitude of robots towards a specific task and to all other tasks from the task table in CMU, preferences are given to the robots which have successfully completed the same task or its portion, whatever was assigned to it, within specific time limit. Also the robots that have shown a positive response to the tasks assigned to them in general, obtain more weight than others. Reallocating tasks to these robots improve the chance of successful completion of a task. Hence, percentage of successfully completed tasks increase along with the decrease in the percentage of reallocated tasks. These are evident from figures 3 and 5. As the number of tasks become huge, percentage of successfully completed tasks decrease (and percentage of reallocated tasks increase) for all the task allocation schemes have been compared here. The reason is possible unavailability of robots with sufficient energy or priority collision among the tasks or shortage of time in certain cases.

As the required number of task reallocation in FESA is much lesser than those in EOTA and ATA, the delay in completion of each task in FESA is lesser than its competitors. It may be noticed from figure 4 that the delay increases with increase in number of tasks for all the schemes compared here. This is due to increased number of job reallocation as a result of huge energy consumption, unavailability of suitable robots etc.

#### IV. COMPLEXITY OF FESA

In this session, I have computed both the time and space complexity of FESA.

##### 4.1 Worst Case Time Complexity

Let, at any point of time, total  $N$  number of robots are there in the system busy with  $K$  number of tasks. So, the number of free robots is  $(N-K)$ . Among those  $K$  tasks, one particular task needs to be reallocated and during that time no other task with higher priority is waiting to be allocated and reallocated. Also assume that at most  $HT$  number of entries may appear in the history table and at most  $FT$  number of entries may be there in  $ptr\_robotarray$  corresponding to each task in the TASK table. The maximum size of task table is  $ST$ .

TRAC has to evaluate the reallocation efficiency of  $(N-K)$  number of available robots. So, the time complexity TC of FESA is as follows:

$$TC = (N-K) f \quad (6)$$

Where  $f$  is the complexity to evaluate reallocation efficiency of each robot.

To compute the residual energy to complete reallocated portion of the task, at most  $(ST+FT)$  number of records in  $ptr\_robotarray$  corresponding to the desired task id needs to be scanned. For determining  $E_R(t)$  and  $E_{thres_R}$  entire ROBOT table should be scanned in worse case. So, the complexity involved in this case is  $N$ . For determining the parameter  $history\_of\_support$ , at most  $HT$  entries in HISTORY table,  $FT$  entries in  $ptr\_robotarray$  in TASK table and the entire task table (for determining the value of  $T_C(A)$ ) should be read in



worst case, resulting into the complexity (HT+FT+ST). Complexity of computing distance\_quotient is  $O(1)$  and the same for computing failure quotient is  $(ST \times FT)$  because at most FT records will have to be scanned for all the tasks in the task table to find out the attitude of a robot towards the tasks given to it, in general, not corresponding to one particular task. So, the overall complexity for determination of parameters of TRAC, is  $(ST+FT+N+HT+FT+ST+ST \times FT)$  i.e.  $(N+HT+2FT+2ST+ST \times FT)$ . As far as the rule base tables are concerned, access to exactly one cell of each table is required resulting into total 3 table accesses. Hence, the overall complexity  $f$  for evaluating the reallocation efficiency of one robot is  $(N+HT+2FT+2ST+ST \times FT+3)$ . So, TC is  $O(N(N-K))$ .

#### 4.2 Worst Case Space Complexity

Space complexity is due to the storage of ROBOT table, HISTORY and TASK table with their respective contributions being N, HT and  $(ST \times FT)$  and three rule base tables each having 25 entries. Hence, the overall space complexity is  $(N+HT+ ST \times FT+75)$  i.e.  $O(N)$ .

### V. CONCLUSION

The proposed method FESA is a fuzzy controlled task allocation-reallocation mechanism that analyzes the reallocation efficiency of a robot based on the history of its behavior, its residual energy along with its energy threshold with respect to the minimum energy required to complete the portion of the task to be reallocated, distance of the new robot from the old one and general tendency of the new robot towards the tasks assigned to it. Extensive simulation has been conducted and results are very promising from the perspective of energy optimization as well as optimization of task execution. In future, I have planned to extend the work by incorporating some real life experiments with different kinds of robots and tasks.

### REFERENCES

- [1] Massart Thierry, Meuter Cedric, V B Laurent. On the complexity of partial order trace model checking, Inform. Process. Lett. 106 (2008) 120-126
- [2] M. Davis, H. Putnam. A computing procedure for quantification theory. Journal of ACM, 7(3)(1960) 201-215.
- [3] Dechter R, Rish I. Directional resolution: the davis-putnam procedure. Proceeding of 4th International Conference on Principles of KR&R, Bonn, Germany: Morgan Kaufmann, (1994) 134-145.
- [4] M. Davis, G. Logemann, D. Loveland, A machine program for theorem proving. Communications of the ACM, 5 (1962) 394-397.
- [5] R. E. Bryant. Graph-based algorithms for boolean function manipulation , IEEE Transactions on Computers, 35 (1986) 677-691.
- [6] H Lin, JG Sun, YM Zhang. Theorem proving based on the extension rule, Journal of Automated Reasoning, 31 (2003) 11-21.
- [7] K Xu, F Boussemart, F Hemery, C Lecoutre. Random constraint satisfaction: easy generation of hard (satisfiable) instances , Artificial Intelligence, 171 (2007) 514-534.