

# NOVEL APPROACH FOR DESIGNING OF S-BOX WITH MULTIBIT PARITY DETECTION SCHEME

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## ABSTRACT

*This paper presents novel approach for designing of AES S-box using combinational logic using Verilog and simulated in Xilinx ISE 13.2. AES is data encryption standard which uses same at Encryption as well as for decryption. AES uses Substitution box was divided into five blocks and are designed by Combinational blocks. So that we can easily analyse faults which are caused by natural/malfunctioning faults.*

**Keywords:** ROM Based S-Box, Combinational Design Of S-Box, Affine Transformation, Isomorphic Transformation

## I. INTRODUCTION

Encryption is the process of converting normal text to unknown format by using algorithm called cipher. The format can be understood for those who having knowledge of encryption and key. There are two types of encryption standards are existed. Those are Data Encryption standard (DES) and Advance encryption standard (AES). The data encryption standard was proposed in November 1967. DES has plain text encrypted into 64 bit blocks with the 56 bit key. The input for the encryption is 64 bit input and 56 bit key and managed to 64 bit blocks to get 64 bit output. Faults which were caused by natural /malfunctioning can be complex to analyse.

AES is advance data standard was proposed in the year 26<sup>th</sup> November 2001 by Joan Daemen and Vincent Rijmen (originally called Rijindael). It normally having bit size 128bits and key size varies from 128,192 and 256 bits. AES algorithm will use same key at encryption as well as for decryption. AES will convert normal text to cipher text after 10 rounds in which encryption will take 4 rounds namely as transformation , sub bytes , shift rows and mixed columns after 10 rounds plain text can be converted to cipher text. This cipher text can be reverse processed in the decryption to get plain text. Sub bytes known as S-box stage in Encryption and Inverse S-box in decryption are nonlinear except all blocks are similar in the Encryption and Decryption. Receiver which is using AES must have to know the key otherwise it will not know how to decrypt the data. Implementation of AES hardware may relts in fault. Data thieves can also try to hack which also results in fault. AES conventional one uses the approach of single bit parity check it has less coverage of fault.

## II. AES ALGORITHM

The proposed AES is similar to the conventional AES but the difference is in construction of S-box which was made by combinational gates. AES algorithm works on 4\*4 matrix element called states. It works on states which is of 8bit length.

The state will undergo following stages namely sub bytes and inverse sub bytes, shift rows, and mix columns, transformations. The AES algorithm represented pictorially as below

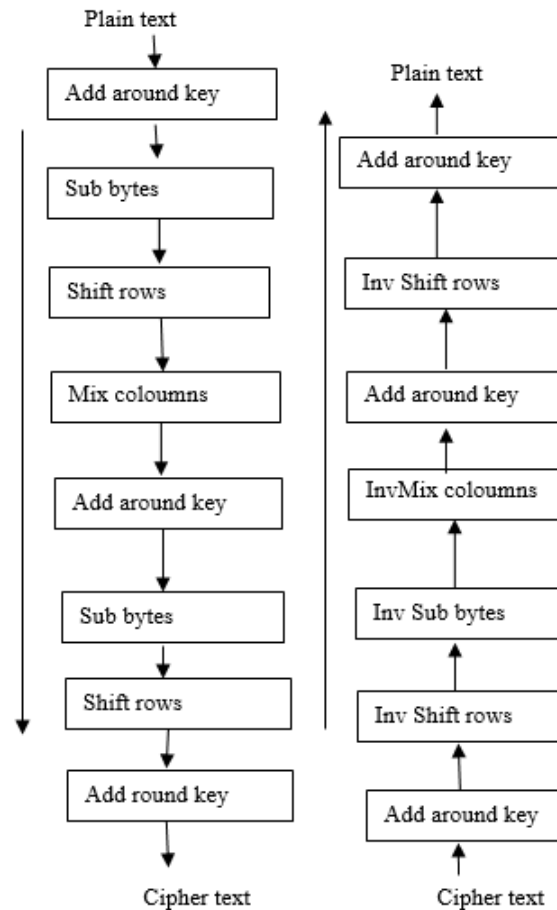


Fig 2.1 AES Algorithm

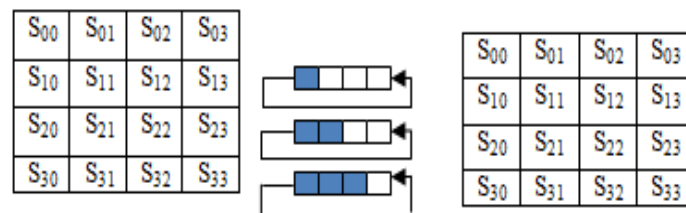
## 2.1 Sub Bytes And Inverse Sub Bytes

These 2 stages are first transformations in their respective round which was performed by byte substitution called sub bytes with 16 s-boxes. In this step each byte in the matrix was replaced by the byte specified in the look up table. The look up table is already with preloaded data

		y															
		0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
x	0	63	7c	77	7b	f2	6b	6f	c5	30	1	67	2b	fe	d7	ab	76
	1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
	2	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
	3	4	c7	23	c3	18	96	5	9a	7	12	80	e2	eb	27	b2	75
	4	9	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
	5	53	d1	0	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
	6	d0	ef	aa	fb	43	4d	33	85	45	f9	2	7f	50	3c	9f	a8
	7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
	8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
	9	60	81	4f	dc	22	29	90	88	46	ee	b8	14	de	5e	0b	db
	a	e0	32	3a	0a	49	6	24	5c	c2	d3	ac	62	91	95	e4	79
	b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	8
	c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
	d	70	3e	b5	66	48	3	f6	0e	61	35	57	ba	86	c1	1d	9e
	e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	ca	ce	55	28	df
	f	sc	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

Fig 2.2 s-box

## 2.2 Shift Rows and Inverse Shift Rows

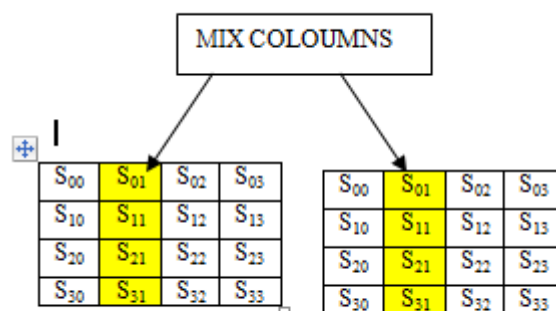


**Figure 2.3 Shift Rows**

In this step encryption side first row left unchanged and second row shifted left to one position and third row shifted by 2 positions similarly last row shifted by three position. At decryption side inverse shift rows were performed as last row shifted by three positions to right, second row shifted by two positions to right, first row is unchanged

## 2.3 Mix Columns and Inverse Mix Columns

In this stage input state byte is multiplied by the fixed polynomial over Galois field and the product value is replaced in output state



**Figure 2.4 Shift Mix Columns**

## 2.4 Add Round Key

Here it was derived from the cipher key using key schedule .each byte in the state matrix is combined with the add round key using Ex-or operation

## 2.5 AES Key Expansion

Aes key takes 4word key as input and produces array of 44 word, each round uses 4 of these words and each word has 32 bytes which means that each sub key is 128 bit long

## III.PROPOSED S-BOX DESIGN

In proposed S-box designion we have designed 5 blocks of hardware. In which 3 blocks represent multiplicative inversion and remaining blocks performs affine transformation. This design also has multi bit

parity fault detection scheme. It will replaces the each single byte in the state matrix so that at time it process a single byte it has 8 bit input and 8 bit output. following block diagram shows the hardware implementation s-box was constured by following formulales of multiplicative inversion and affine transformation for inverse s-box invere multiplicative and inverse affine transformation

### 3.1 Isomorphic and inverse Iso morphic transformations

Multiplicative inverse of an element in  $GF(8)$  can be found by decomposing the element in galosifield into smaller order elements of  $GF(2)$ ,  $GF(2^1)$  and  $GF(2^2)$ . Multiplicative inverse of an element composite field can be found by mapping an element using isomorphic function then we find multiplicative inversion and again converted back to composite field by using inverse isomorphic function which was denoted by  $\delta$  is an  $8 \times 8$  matrix and multiplication is AND operation, addition is modulo-2 addition

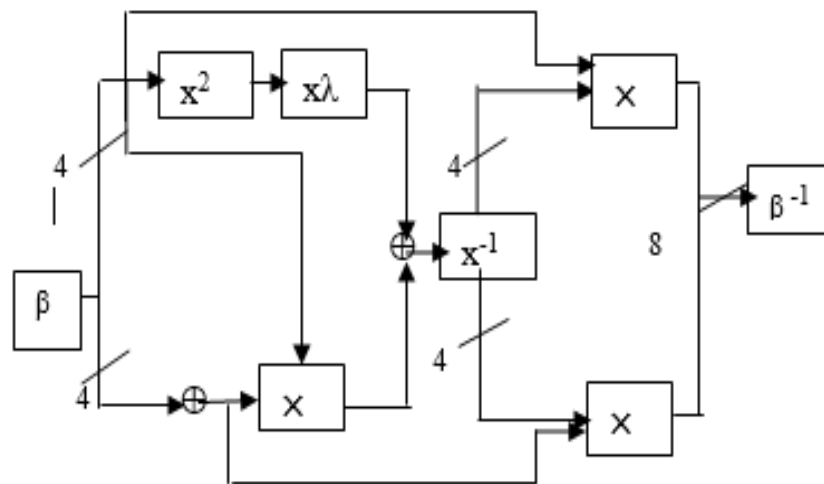


Fig 3.1 Block diagram of s-box

- $\beta \rightarrow$  iso morphic transformation
- $\times \rightarrow$  multiplication
- $x\lambda \rightarrow$  multiplication with lambda
- $x^2 \rightarrow$  squarer
- $\delta^{-1} \rightarrow$  inverse iso morphic transformation
- $X^{-1} \rightarrow$  Multiplicative inversion

#### 1. Isomorphic and inverse Iso morphic transformations

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Where q is 8 bit incoming data

$$\beta \times q = \begin{pmatrix} 10100000 \\ 11011110 \\ 10101100 \\ 10101110 \\ 11000110 \\ 10011110 \\ 01010010 \\ 01000011 \end{pmatrix} \times \begin{pmatrix} q7 \\ q6 \\ q5 \\ q4 \\ q3 \\ q2 \\ q1 \\ q0 \end{pmatrix} = \beta^{-1} \times q = \begin{pmatrix} 11100010 \\ 01000100 \\ 01100010 \\ 01110110 \\ 00111110 \\ 10011110 \\ 00110000 \\ 01110101 \end{pmatrix} \times \begin{pmatrix} q7 \\ q6 \\ q5 \\ q4 \\ q3 \\ q2 \\ q1 \\ q0 \end{pmatrix}$$

$$\delta \times q = \begin{pmatrix} q7 \oplus q5 \\ q7 \oplus q6 \oplus q4 \oplus q3 \oplus q2 \oplus q1 \\ q7 \oplus q5 \oplus q3 \oplus q2 \\ q7 \oplus q5 \oplus q3 \oplus q2 \oplus q1 \\ q7 \oplus q5 \oplus q3 \oplus q2 \\ q7 \oplus q6 \oplus q2 \oplus q1 \\ q7 \oplus q4 \oplus q3 \oplus q2 \oplus q1 \\ q6 \oplus q4 \oplus q1 \\ q6 \oplus q1 \oplus q0 \end{pmatrix} \quad \delta^{-1} \times q = \begin{pmatrix} q7 \oplus q6 \oplus q5 \oplus q1 \\ q6 \oplus q2 \\ q6 \oplus q5 \oplus q1 \\ q6 \oplus q5 \oplus q4 \oplus q2 \oplus q1 \\ q5 \oplus q4 \oplus q3 \oplus q2 \oplus q1 \\ q7 \oplus q4 \oplus q3 \oplus q2 \oplus q1 \\ q5 \oplus q4 \\ q6 \oplus q5 \oplus q4 \oplus q2 \oplus q0 \end{pmatrix}$$

### 3.2 Affine Transformation

Affine transformation and its inverse was found after finding multiplicative inverse since its inputs are multiplicative inverse of 8 bit input byte in sste matrix ,both affine and its inverse was using same multiplicative inverse and is denoted by matrix “a”

$$AT(a) = \begin{pmatrix} 11111000 \\ 01111100 \\ 00111110 \\ 00011111 \\ 10001111 \\ 11000111 \\ 11100011 \\ 11110001 \end{pmatrix} \times \begin{pmatrix} a7 \\ a6 \\ a5 \\ a4 \\ a3 \oplus \\ a2 \\ a1 \\ a0 \end{pmatrix} \begin{pmatrix} 0 \\ 1 \\ 1 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \end{pmatrix} \quad AT^{-1}(a) = \begin{pmatrix} 01010010 \\ 00101001 \\ 10010100 \\ 01001010 \\ 00100101 \\ 10010010 \\ 01001001 \\ 10100100 \end{pmatrix} \times \begin{pmatrix} a7 \\ a6 \\ a5 \\ a4 \oplus \\ a3 \\ a2 \\ a1 \\ a0 \end{pmatrix} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \\ 1 \end{pmatrix}$$

### 3.3 Airthemetic Operations In Galoisi Field

#### i. Multiplication with constant, $\lambda$

Here the input is 4 bit and and constant is denoted by  $\lambda = \{1100\}$  we will multiply the isomorphic output was first squared then that 4 bit output fed multiplier unit that can be performed by following formulae.

$$k3 = q2 \oplus q0;$$

$$k2 = q3 \oplus q2 \oplus q1 \oplus q0;$$

$$k1 = q3;$$

$$k0 = q2;$$

#### ii. Squaring in $GF(2^4)$

we can calculate squaring by letting  $k = q^2$ , where  $k$  and  $q$  are elements in  $GF(2^2)$  and  $k, q$  are denoted by binary numbers  $\{k3k2k1k0\}, \{q3q2q1q0\}$  respectively and squaring can be found by using following formulae which are deduced by using decomposition

$$k3 = q3$$

$$k2 = q3 \oplus q2;$$

$$k1 = q1 \oplus q2;$$

$$k0 = q3 \oplus q1 \oplus q0;$$

#### iii. $GF(2^2)$ Multiplication

Let  $k = qw$ , where  $k = \{k1 k0\}_2$ ,  $q = \{q1 q0\}_2$  and  $w = \{w1 w0\}_2$  are elements of  $GF(2^2)$ .

$$k1 = q1 w1 \oplus q0 w1 \oplus q1 w0;$$

$$k2 = q1 w1 \oplus q0 w0;$$

#### iv. Multiplication with constant $\phi$

Let  $k = q\phi$ , where  $k = \{k1 k0\}_2$ ,  $q = \{q1 q0\}_2$  and  $\phi = \{10\}_2$  are elements of  $GF(2^2)$ .

$$K1 = q1 \oplus q0;$$

$$K0 = q0;$$

### 3.4 Multiplicative Inversion

The multiplicative inverse of  $q$  (where  $q$  is element of  $GF(24)$ ) such that  $q^{-1} = \{q3^{-1}, q2^{-1}, q1^{-1}, q0^{-1}\}$ .

$$q3^{-1} = q3 \oplus q3q2q1 \oplus q3q0 \oplus q2;$$

$$q2^{-1} = q3q2q1 \oplus q3q2q0 \oplus q3q0 \oplus q2 \oplus q1;$$

$$q1^{-1} = q3 \oplus q3q2q1 \oplus q3q1q0 \oplus q2 \oplus q2q0 \oplus q1;$$

$$q0^{-1} = q3q2q1 \oplus q3q2q0 \oplus q3q1 \oplus q3q1q0 \oplus q3q0 \oplus q2 \oplus q2q1 \oplus q2q1q0 \oplus q1 \oplus q0;$$

#### IV. FAULT DETECTION METHOD

In prior designs of AES have fault detection schemes of single bit in this proposed design of s-box and inverse s-box was divided into 5 blocks. parity of each block was identified from the input bits of the blocks. we can evaluate the parities of each block as follows

*For block 1 & block 5*

Let  $z$  be an input of s-box. The initial block of s-box consisting of transformation of matrices. Which was done by using isomorphic transformation its predicted parity calculated as follows and denoted by  $p_1$ , block 5 having inverse transformation of the matrices which is inverse isomorphic transformation and its parity denoted as  $p_5$  and its input denoted by  $V$

$$P_1 = Z[0] + Z[2] + Z[4] + Z[5];$$

$$P_5 = V[0] + V[1] + V[2] + V[4] + V[6];$$

*For block 2 & 4*

Block 2 and 4 comprises of modulo-2 adder, multiplication with  $\lambda$  and multiplier and squarer each having 4 bit and 8 bit input according to their role their parities are denoted by  $p_2, p_4$  respectively

$$P_2 = E[4] + E[3] ((\sim Ph) + E[6]) + (\sim E[2] (ph + e[6]) + e[1] e[6] + e[4]) + E[0] (\sim ph) ;$$

$$P_4 = e[3] (s[0] + s[2] + e[2] s[0] + s[1] + s[3]) + e[1] (s[6] + s[4] + e[0] s[0] + s[1] + s[2] + s[3]) ;$$

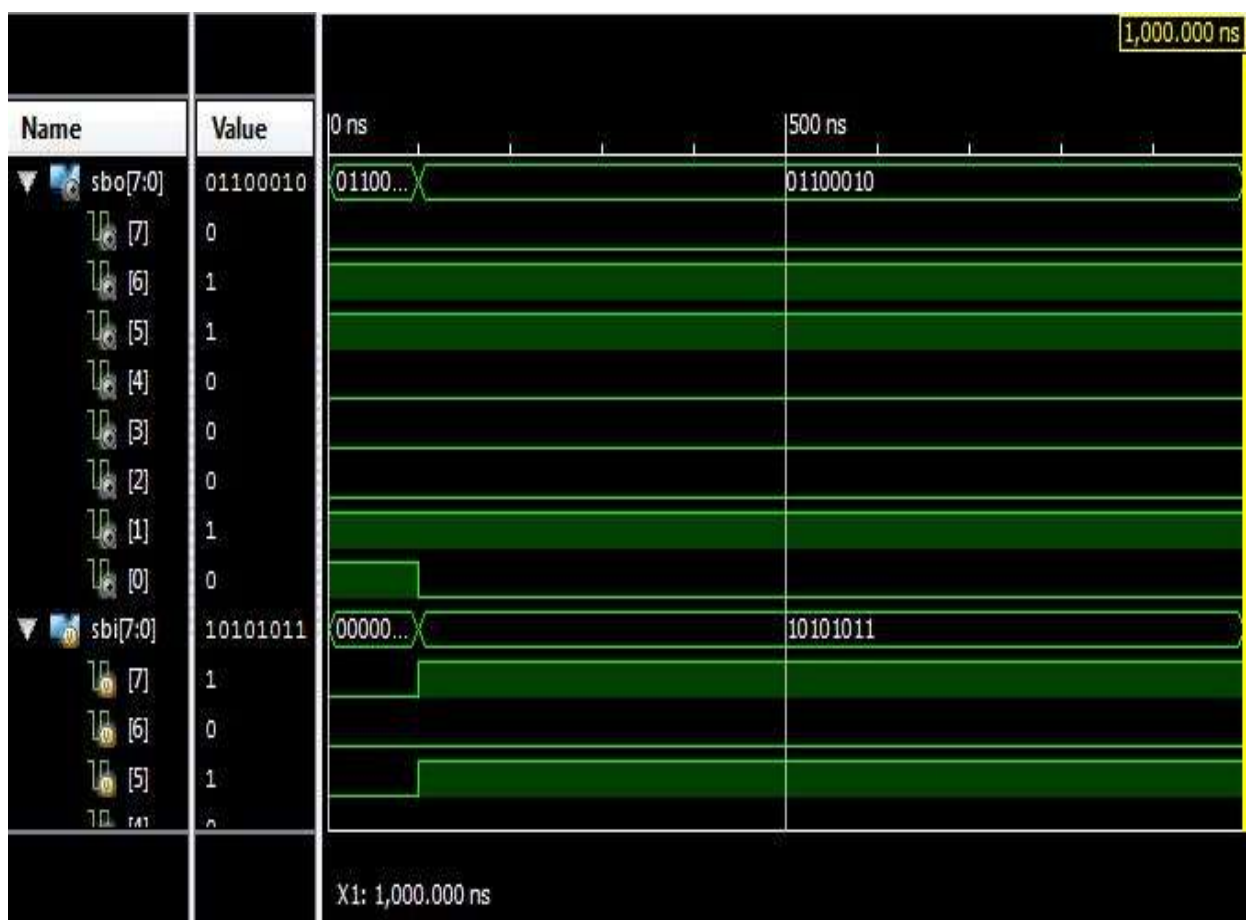
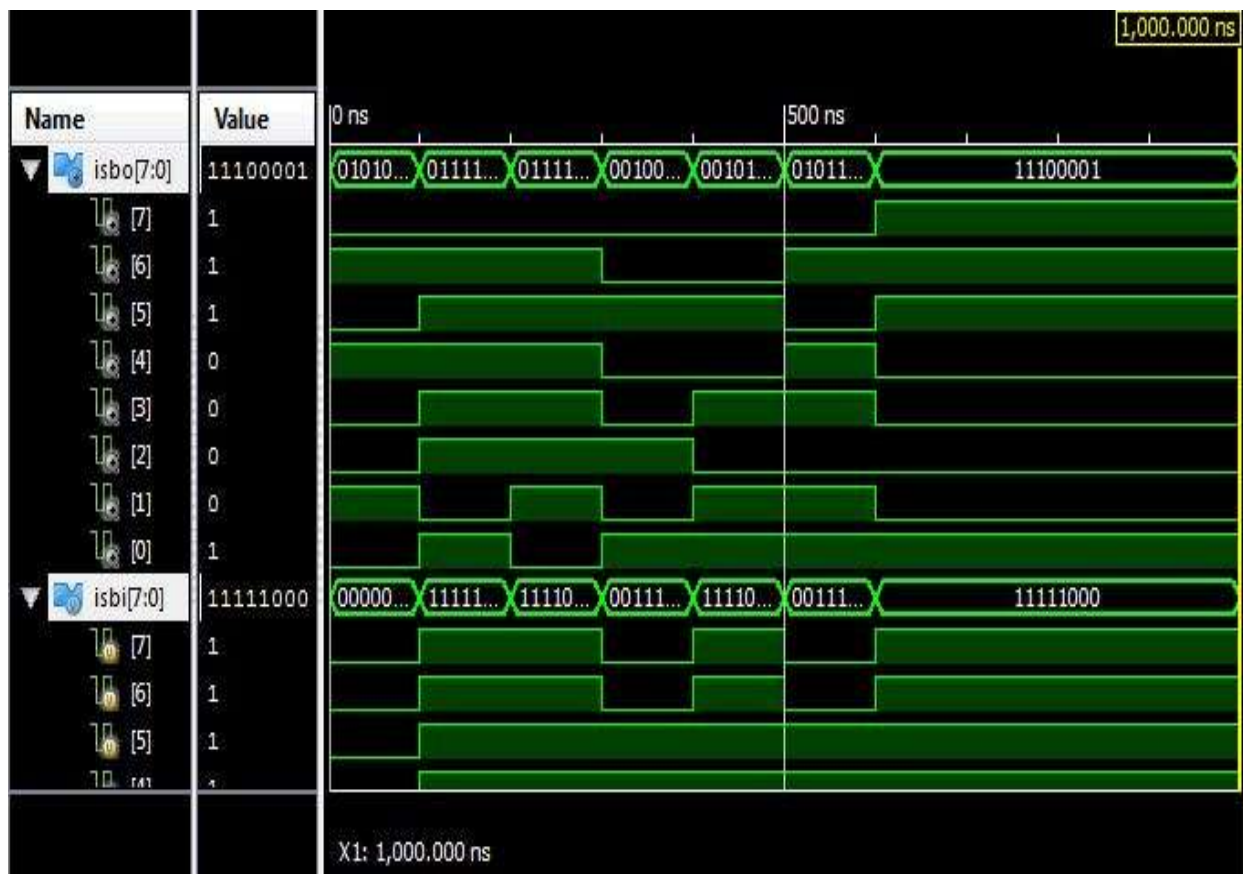
*Block 3*

This block performs multiplicative inverse on the given input data. it accepts 4bit input and perform multiplicative inverse and produce 4 bit output. This block parity can be found by given formulae

$$P_3 = (r_1 + r_0) r_3 + (\sim r_2 | r_1) r_0;$$

#### V. SIMULATION RESULTS

The S-box is designed in Verilog HDL and simulated in the Xilinx ISE13.2I. This design is combinational design which reduces the hardware design complexity. Which enhances the speed. The complexity less.








## VI. CONCLUSION

This type of novel design of s-box using combinational logic with the multi Obit fault detection scheme was designed using Verilog hardware description language with 8bit input and simulated in Xilinx ISE 13.2 found that novel design giving better performance and reduced area due to galosifield operations in combinational design.

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