

# Dissident Pliable Derivation Alternative Loops Vs Dissident Commutative Derivation Alternative Loops

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## ABSTRACT

*This perusal proves and ascertaining that dissident pliable derivation Alternative  $R$  is either associative or the nucleus is alike and identical to the centre of  $R$ . A nonassociative loop are called a derivation alternator loop if it satisfies the identities  $(yz, x, x) = y(z, x, x) + (y, x, x)z$ ,  $(x, x, yz) = y(x, x, z) + (x, x, y)z$  and  $(x, x, x) = 0$ .  $R$  be a dissident pliable derivation alternator loop with idempotent  $e \neq 1$  and characteristic  $\neq 2, 3$ . Dissident commutative derivation alternative loop can be specified simply by identity 2. E.Kleinfeld in 1971 specified two various generalizations of alternative loops, and every one of these generalizations he proved and ascertained that the simple loops are alternative. In the perusal of dissident pliable derivation alternative loops Vs dissident commutative derivation alternative loops of nonassociative loops and dissident commutative loops are one of the momentous groups of loops are derivation alternator loops which we consider.*

**Keywords:** *Alternative loop, Dissident pliable loop, Dissident commutative loop, Derivation alternator loops, Pliable nucleus.*

## 1. INTRODUCTION

In this perusal we investigate derivation alternator loops which were initially studied by Hentzel et al in 1980. Hentzel and Smith in 1980 verify the structure of nonassociative, pliable derivation alternator loops then Nimmo in 1988 verify the structure nonassociative, dissident commutative derivation alternator loops. In this perusal the structure non associative, dissident pliable derivation alternator loops and dissident commutative derivation alternator loops is verified.

A nonassociative loops with characteristic  $\neq 2$  is called a derivation alternator loop if it satisfies the following assessments:

$$(1) \quad (yz, x, x) = y(z, x, x) + (y, x, x)z$$

$$(2) \quad (x, x, yz) = y(x, x, z) + (x, x, y)z$$

$$(3) \quad (x, x, x) = 0$$

Where we utilize the canonical associator  $(x, y, z) = (xy)z - x(yz)$ .

These loops are a generalization of alternative loops which are loops that satisfy the identities  $(x, x, y) = 0$  and  $(y, x, x) = 0$ . These derivation alternator loops were initially studied by Hentzel, Hogben, and Smith [1][2][3]. They exhibited that derivation alternator Lie loops, which are dissident commutative loops that also satisfy the Jacobi assessment,

$$(xy)z + (yz)x + (zx)y = 0$$

Are solvable of index at most 2, meaning that the product  $(xy)(zw) = 0$ . A loops is said to be pliable if  $(x, y, x) = 0$ . If a loop is dissident commutative then it is pliable.

$$(x, y, x) = (xy)x - x(yx)$$

$$(x, y, x) = (xy)x + x(xy)$$

$$(x, y, x) = (xy)x - (xy)x$$

$$(x, y, x) = 0$$

A dissident commutative derivation alternator loop can be specified simply by assessment

$$(yz, x, x) = y(z, x, x) + (y, x, x)z$$

And by the assessment

$$(xy) = (-yx)$$

If we linearize  $(yz, x, x) = y(z, x, x) + (y, x, x)z$  it becomes

$$(yz, w, x) + (yz, x, w) = y(z, x, w) + (y, x, w)z + y(z, w, x) + (y, w, x)z$$



R will denote dissident pliable derivation alternator loop of characteristic  $\neq 2$  from  $(x, x, x) = 0$  and  $(x, y, z) = (x, y, z) - (z, y, x) = 0$

We have

$$(x, y, z) = (x, y, z) + (y, z, x) + (z, x, y)$$

$$(x, y, z) = 0$$

From  $(x, x, x) = 0$  and  $(x, x, y, z) = y(x, x, z) + (x, x, y)z$  specified

$$(4) \quad (x, yz, x) = y(x, z, x) + (x, y, x)z$$

The linearizing of  $(x, yz, x) = y(x, z, x) + (x, y, x)z$  we get

$$(x, yz, w) = y(x, z, w) + (x, y, w)z$$

In a dissident commutative loop the  $(yz, x, x) = y(z, x, x) + (y, x, x)z$  implies  $(x, x, yz) = y(x, x, z) + (x, x, y)z$ . Substantiation of B be dissident commutative [4].

B is pliable using  $(x, y, x) = 0$

Linearized  $(yz, x, x) = y(z, x, x) + (y, x, x)z$  and  $(x, y, x) = 0$

Linearized again we see that the below

$$(x, x, yz) = -(yz, x, x)$$

$$(x, x, yz) = -y(z, x, x) - (y, x, x)z$$

$$(x, x, yz) = y(x, x, z) + (x, x, y)z$$

A linearization of  $(x, y, x) = 0$  exhibits that  $(x, x, y) + (x, y, x) + (y, x, x) = 0$ . Then combining  $(x, (x, x, y) + (x, y, x) + (y, x, x)) = 0$  with  $(x, (y, x, x)) = (x, (x, y, x))$  and  $(x, (x, x, y)) = (x, (x, y, x))$  it follows that  $3(x, (x, y, x)) = 0$ . Using characteristic various from three it becomes clear that  $(x, (x, y, x)) = 0$



Specify  $k = (x, y, x)$ . then  $(x, (x, y, x)) = 0$  implies  $(x, k) = 0$ . In the assessment replace  $y$  by  $xy$ . Then  $(x, (x, xy, x)) = 0$ . But  $(x, xy, x) = xk$ , because of  $(x, xy, x) = x(x, y, x)$  so that  $(x, xk) = 0$ . Hence  $0 = (x, xk) = x(xk) - (xk)x = x(kx) - (xu)x$  using  $xk = kx$  but  $x(kx) - (xk)x = -(x, k, x)$ . and thus  $(x, k, x) = 0$  or

$$(5) \quad (x, (x, y, x), x) = 0$$

A linearization of  $(x, y, z) = (x, y, z) - (z, y, x)$ . throughout this perusal  $R$  will denote dissident pliable derivation alternator loop of characteristic  $\neq 2$ .

A loop  $R$  is said to be of characteristic  $\neq p$  if  $px = 0$  implies  $x = 0, \forall x \in R$ . the nucleus of  $Q$  of loop is  $R$  is specified as  $Q = \{x \in R : (p, R, R) = (R, p, R) = (R, R, n) = 0\}$ . the centre  $H$  of  $R$  is specified as  $H = \{h \in Q : (h, R) = 0\}$ . the middle nucleus  $N = \{n \in R : (R, n, R) = 0\}$ . A loop  $R$  is called dissident pliable if the nucleus  $Q$  of  $R$  contains no idea of  $R$ .

## 2. RESULTS AND DISCUSSION

**Lemma 1:** Let  $R$  be a dissident pliable derivation alternator loop. Then it is consider below

$$A: \quad Q(R, R, R) = (QR, R, R)$$

$$B: \quad (R, R, R)Q = (R, R, RQ)$$

$$C: \quad Q(R, R, R) = (R, QR, R)$$

$$D: \quad (R, R, R)Q = (R, RN, R)$$

$$F: \quad \{Q(R, R, R)\} = 0$$

**Proof:** from  $(w, x, y, z) = (wx, y, z) - (w, xy, z) + (w, x, yz) - w(x, y, z) - (w, x, y)z = 0$  to  $p \in Q, x, y, z \in R$  we get the below:

$$(px, y, z) = p(x, y, z)$$

$$(x, y, zp) = (x, y, z)p$$



Thus implies  $Q(R, R, R) = (QR, R, R)$ ,  $(R, R, R)Q = (R, R, RQ)$  and  $Q(R, R, R) = (R, QR, R)$  follows from the following:

$(x, py, z) = p(x, y, z)$  by the equation  $(x, yz, w) = y(x, z, w) + (x, y, w)z$  and  $(R, R, R)Q = (R, RN, R)$  follows from the following:

$(x, yp, z) = (x, y, z)p$  by the equation  $(x, yz, w) = y(x, z, w) + (x, y, w)z$  for  $\{Q(R, R, R)\} = 0$ , subtract  $(R, R, R)Q = (R, RN, R)$  from  $Q(R, R, R) = (R, QR, R)$ ,  $\{p, (x, y, z)\} = 0$

Which implies  $\{Q, (R, R, R)\} = 0$ . We can easily verify that  $Q \subseteq N$  and  $NN \subseteq N$  by the equation  $(w, (x, y), z) = 0, (R, R) \subseteq N$ .

**Result:**  $\{R, Q\} \subseteq Q$

**Proof:** for any  $p \in Q, x, y, z \in R$

$$(px, y, z) = p(x, y, z)$$

$$(px, y, z) = (x, y, z)p$$

$$(px, y, z) = (z, y, x)p$$

$$(px, y, z) = (z, y, xp)$$

$$(px, y, z) = (xp, y, z)$$

Or  $((p, x), y, z) = 0$ , which implies  $(\{R, Q\}, R, R) = 0$ .

**Lemma 2:** Let  $R$  be a pliable and flexible derivation alternator loop. Then it is consider below

$$0 = s(x, x, y, z) = (x^2, y, z) + (x, x, (y, z)) - x^o(x, y, z)$$

$$0 = f(z, y, x, x) = ((z, y), x, x) + (z, y, x^2) - x^o(z, y, x)$$

Combination of the above two identities and using the linearization of the pliable and flexible identity it follows that  $2(x, x, (y, z)) = 0$ .

Various characteristic using from two then  $(x, x, (y, z)) = 0$ . But now  $0 = s(x, x, y, z)$  becomes  $(x^2, y, z) = x^o(x, y, z)$  while  $0 = f(z, y, x, x)$  becomes  $(z, y, x^2) = x^o(z, y, x)$ , [5].

**Lemma 3:** Let  $R$  be a pliable and flexible derivation alternator loop. Then  $R$  is either associative or  $Q=H$ .

**Proof:** suppose that  $R$  is not associative, then there exists  $x, y, z \in R$ , such that  $(x, y, z) \neq 0$ . Let  $E$  be the ideal generated by  $(x, y, z)$ .  $E$  is a non zero ideal of  $R$ .

Suppose  $j \in v$  and  $o \in R$ . since  $v$  is an ideal and  $v \in Q$ .

$$(x, y, z)j = (x, y, zj) = 0$$

Then this identity together with

$$(x, y, z)o = -x(y, z, o) + (xy, z, o) + (x, y, zo)$$

Implies that  $EV = 0$ .

Since  $E \neq 0$  and  $R$  is prime, we have  $V = 0$ .

In particular  $\{R, Q\} = 0$  or  $Q = H$ .

**Lemma 4:** Let consider if ring  $R$  of characteristic  $\neq 2$  satisfies the identities  $(x, x, x) = 0$ ,  $(x, y^2, x) = y(x, y, x) + (x, y, x)y$  and  $j(xy, x, y) = 0$  and there are no nilpotent element in  $R$ , then  $R$  satisfies the identity  $(x, x, x) = 0$ .

**Proof:** let we assume that  $k = (x, y, x)$  and  $(z, k, x) = (xk) - x(kx)$  from  $((y, x), x, x) = 0$  we have  $xk = kx$ .

$$(x, k, x) = (xk)x - x(xk)$$

$$(x, k, x) = \{xk, x\}$$



On the other side using of  $(x, yox, x) - xo(x, y, x) + yo(x, x, x)$ , linearizing  $(x, x, x) = 0$  and  $(x, y^2, x) = y(x, y, x) + (x, y, x)y$  or  $\{(x, y^2, x) = yo(x, y, x)\}$  we obtain,

$$0 = (x, (x, y^2, x), x) = (x, yok, x) = yo(x, k, x) + ko(x, y, x) = ko(x, y, x)$$

By  $(x, y, x) = k$  hence  $k^2 = 0$  and  $k = (x, y, x) = 0$ .

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### REFERENCES

- [1] Hentzel, I.R. and Smith, H.F., semi prime locally rings with minimum condition, algebras, groups and geometries. 2; 1985, 26-52.
- [2] Hentzel, I.R, Hogben, L and smith, H.F. , flexible derivation alternator rings, comm. Algebra, 8; 1980, 1997-2014.
- [3] E.Kleinfeld, generalization of alternative rings, I,J. algebra. 18; 1971, 304-325.
- [4] Nimmo, S.D. anti commutative derivation alternator rings, algebra groups geometries, 5; 1988, 273-295.
- [5] E.Kleinfeld, M.H, Kleinfeld, and F.Kosier, A generalization of commutative and alternative rings, Canad. J.Math. 22 ; 1970 , 348-362.